

# Intuitionistic Fuzzy $\gamma$ Supra Open Mappings And Intuitionistic Fuzzy $\gamma$ Supra Closed Mappings

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**Abstract**-Necla Turanl introduced the concept of Intuitionistic fuzzy supra topological space which is a special case of Intuitionistic fuzzy topological space. Aim of this paper is we introduced in IF  $\gamma$  supra open sets in Intuitionistic fuzzy supra topological space. and also we studied about Intuitionistic Fuzzy  $\gamma$  Supra Open Mappings And Intuitionistic Fuzzy  $\gamma$  Supra Closed Mappings in Intuitionistic fuzzy supra topological spaces

**Index Terms**-IF $\gamma$  supra open set, IF $\gamma$  supra closed set, Intuitionistic fuzzy  $\gamma$  supra Open Mappings, Intuitionistic fuzzy  $\gamma$  supra Closed Mappings

## 1. INTRODUCTION

Topology is a classical subjects, as a generalization topological spaces many type of topological spaces introduced over the year. C.L. Chang [4] was introduced and developed fuzzy topological space by using L.A. Zadeh's [23] fuzzy sets. Coker [5] introduced the notion of Intuitionistic fuzzy topological spaces by using Atanassov's [2] Intuitionistic fuzzy sets

A.S. Mashhour [13] et al. Introduced and studied the supra topological spaces in the year 1983. M. E. AbdEl-Monsef et al. [1] introduced the fuzzy supra topological spaces and studied fuzzy supra-continuous functions and obtained some properties and characterizations. In 2003 Necla Turanl [21] introduced the concept of Intuitionistic fuzzy supra topological space

In 1996 D. Andrijevic [2] introduced b open sets in topological space. In this paper we introduced and studied about Intuitionistic Fuzzy  $\gamma$  Supra Open Mappings And Intuitionistic Fuzzy  $\gamma$  Supra Closed Mappings in Intuitionistic fuzzy supra topological spaces

## 2. PRELIMINARIES

**Definition 2.1:** [3]

An Intuitionistic fuzzy set (IF for short) A is an object having the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$$

where the functions  $\mu_A: X \rightarrow [0,1]$  and  $\nu_A: X \rightarrow [0,1]$  denote the degree of membership (namely  $\mu_A(x)$ ) and

the degree of non-membership (namely  $\nu_A(x)$ ) of each element  $x \in X$  to the set A respectively, and  $0 \leq \mu_A(x) + \nu_A(x) \leq 1$  for each  $x \in X$ .

Obviously, every fuzzy set A on a nonempty set X is an IFS of the following form

$$A = \{ \langle x, \mu_A(x), 1 - \mu_A(x) \rangle : x \in X \}.$$

**Definition 2.2**[3]

Let A and B be two IFSs of the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \} \text{ and } B = \{ \langle x, \mu_B(x), \nu_B(x) \rangle : x \in X \}.$$

Then,  
(i)  $A \subseteq B$  if and only if  $\mu_A(x) \leq \mu_B(x)$  and  $\nu_A(x) \geq \nu_B(x)$  for all  $x \in X$ ,

(ii)  $A = B$  if and only if  $A \subseteq B$  and  $A \supseteq B$ ,

(iii)  $A^c = \{ \langle x, \nu_A(x), \mu_A(x) \rangle : x \in X \}$ ,

(iv)  $A \cup B = \{ \langle x, \mu_A(x) \vee \mu_B(x), \nu_A(x) \wedge \nu_B(x) \rangle : x \in X \}$ ,

(v)  $A \cap B = \{ \langle x, \mu_A(x) \wedge \mu_B(x), \nu_A(x) \vee \nu_B(x) \rangle : x \in X \}$ .

(vi)  $\emptyset = \{ \langle x, \mu_A(x), 1 - \mu_A(x) \rangle : x \in X \}$ ;

(vii)  $X = \{ \langle x, 1 - \nu_A(x), \nu_A(x) \rangle : x \in X \}$ ;

The Intuitionistic fuzzy sets  $0 \sim = \langle x, 0, 1 \rangle$  and  $1 \sim = \langle x, 1, 0 \rangle$  are respectively the empty set and the whole set of X

**Definition 2.3.** [3]

Let  $\{A_i : i \in J\}$  be an arbitrary family of IFS Intuitionistic fuzzy sets in X. Then

(i)  $\bigcap A_i = \{ \langle x, \bigwedge \mu_{A_i}(x), \bigvee \nu_{A_i}(x) \rangle : x \in X \}$ ;

(ii)  $\bigcup A_i = \{ \langle x, \bigvee \mu_{A_i}(x), \bigwedge \nu_{A_i}(x) \rangle : x \in X \}$ .

**Definition 2.4.** [3]

Since our main purpose is to construct the tools for developing Intuitionistic fuzzy topological spaces, we must introduce the Intuitionistic fuzzy sets  $0 \sim$  and  $1 \sim$  in X as follows:

$0\sim = \{ \langle x, 0, 1 \rangle : x \in X \}$  and  $1\sim = \{ \langle x, 1, 0 \rangle : x \in X \}$ .

**Definition 2.5[3]**

Let  $A, B, C$  be Intuitionistic fuzzy sets in  $X$ . Then

- (i)  $A \subseteq B$  and  $C \subseteq D \Rightarrow A \cup C \subseteq B \cup D$  and  $A \cap C \subseteq B \cap D$ ,
- (ii)  $A \subseteq B$  and  $A \subseteq C \Rightarrow A \subseteq B \cap C$ ,
- (iii)  $A \subseteq C$  and  $B \subseteq C \Rightarrow A \cup B \subseteq C$ ,
- (iv)  $A \subseteq B$  and  $B \subseteq C \Rightarrow A \subseteq C$ ,
- (v)  $\overline{A \cup B} = \overline{A} \cap \overline{B}$
- (vi)  $\overline{A \cap B} = \overline{A} \cup \overline{B}$ ,
- (vii)  $A \subseteq B \Rightarrow \overline{B} \subseteq \overline{A}$ ,
- (viii)  $\overline{\overline{A}} = A$ ,
- (ix)  $\overline{1\sim} = 0\sim$ ,
- (x)  $\overline{0\sim} = 1\sim$ .

**Definition 2.6[3]**

Let  $f$  be a mapping from an ordinary set  $X$  into an ordinary set  $Y$ ,

If  $B = \{ \langle y, \mu_B(y), \nu_B(y) \rangle : y \in Y \}$  is an IFST in  $Y$ , then the inverse image of  $B$  under  $f$  is an IFST defined by  $f^{-1}(B) = \{ \langle x, f^{-1}(\mu_B)(x), f^{-1}(\nu_B)(x) \rangle : x \in X \}$

The image of IFST  $A = \{ \langle y, \mu_A(y), \nu_A(y) \rangle : y \in Y \}$  under  $f$  is an IFST defined by

$f(A) = \{ \langle y, f(\mu_A)(y), f(\nu_A)(y) \rangle : y \in Y \}$ .

**Definition 2.7[3]**

Let  $A, A_i (i \in J)$  be Intuitionistic fuzzy sets in  $X$ ,  $B, B_i (i \in K)$  be Intuitionistic fuzzy sets in  $Y$  and  $f: X \rightarrow Y$  is a function. Then

- (i)  $A_1 \subseteq A_2 \Rightarrow f(A_1) \subseteq f(A_2)$ ,
- (ii)  $B_1 \subseteq B_2 \Rightarrow f^{-1}(B_1) \subseteq f^{-1}(B_2)$ ,
- (iii)  $A \subseteq f^{-1}(f(A))$  { If  $f$  is injective, then  $A = f^{-1}(f(A))$  },
- (iv)  $f(f^{-1}(B)) \subseteq B$  { If  $f$  is surjective, then  $f(f^{-1}(B)) = B$  },
- (v)  $f^{-1}(\cup B_j) = \cup f^{-1}(B_j)$
- (vi)  $f^{-1}(\cap B_j) = \cap f^{-1}(B_j)$
- (vii)  $f(\cup B_j) = \cup f(B_j)$
- (viii)  $f(\cap B_j) \subseteq \cap f(B_j)$  { If  $f$  is injective, then  $f(\cap B_j) = \cap f(B_j)$  }
- (ix)  $f^{-1}(1\sim) = 1\sim$ ,
- (x)  $f^{-1}(0\sim) = 0\sim$ ,
- (xi)  $f(1\sim) = 1\sim$ , if  $f$  is surjective
- (xii)  $f(0\sim) = 0\sim$ ,
- (xiii)  $\overline{f(A)} \subseteq f(\overline{A})$ , if  $f$  is surjective,
- (xiv)  $f^{-1}(\overline{B}) = \overline{f^{-1}(B)}$ .

**Definition 2.8[21]**

A family  $\tau_\mu$  Intuitionistic fuzzy sets on  $X$  is called an Intuitionistic fuzzy supra topology (in short, IFST) on  $X$  if  $0\sim \in \tau_\mu, 1\sim \in \tau_\mu$  and  $\tau_\mu$  is closed under arbitrary suprema.

Then we call the pair  $(X, \tau_\mu)$  an Intuitionistic fuzzy supra topological space (in short, IFSTS).

Each member of  $\tau_\mu$  is called an Intuitionistic fuzzy supra open set and the complement of an

Intuitionistic fuzzy supra open set is called an Intuitionistic fuzzy supra closed set.

**Definition 2.9[21]**

The Intuitionistic fuzzy supra closure of a set  $A$  is denoted by  $S-cl(A)$  and is defined as

$S-cl(A) = \cap \{ B : B \text{ is Intuitionistic fuzzy supra closed and } A \subseteq B \}$ .

The Intuitionistic fuzzy supra interior of a set  $A$  is denoted by  $S-int(A)$  and is defined as

$S-int(A) = \cup \{ B : B \text{ is Intuitionistic fuzzy supra open and } A \supseteq B \}$

**Definition 2.10[21]**

- (i).  $\neg(AqB) \Leftrightarrow A \subseteq B^C$ .
- (ii).  $A$  is an Intuitionistic fuzzy supra closed set in  $X \Leftrightarrow S-cl(A) = A$ .
- (iii).  $A$  is an Intuitionistic fuzzy supra open set in  $X \Leftrightarrow S-int(A) = A$ .
- (iv).  $S-cl(A^C) = (S-int(A))^C$ .
- (v).  $S-int(A^C) = (S-cl(A))^C$ .
- (vi).  $A \subseteq B \Rightarrow S-int(A) \subseteq S-int(B)$ .
- (vii).  $A \subseteq B \Rightarrow S-cl(A) \subseteq S-cl(B)$ .
- (viii).  $S-cl(A \cup B) = S-cl(A) \cup S-cl(B)$ .
- (ix).  $S-int(A \cap B) = S-int(A) \cap S-int(B)$ .

**Definition 2.11**

Let  $(X, \tau_\mu)$  is a Intuitionistic fuzzy supra topological space and  $A \subseteq X$ . Then  $A$  is said to be Intuitionistic fuzzy  $\gamma$  supra open (briefly IF $\gamma$ s -open) set if  $A \subseteq s-cl(S-int(A)) \cup S-int(s-cl(A))$ .

The complement of Intuitionistic fuzzy  $\gamma$  supra open set is called Intuitionistic fuzzy  $\gamma$  supra closed set (briefly IF $\gamma$ s closed).

**Definition 2.12**

The Intuitionistic fuzzy  $\gamma$  supra closure of a set  $A$  is denoted by  $IF\gamma S-cl(A)$  and is defined as

$IF\gamma S-cl(A) = \cap \{ B : B \text{ is Intuitionistic fuzzy } \gamma \text{ supra closed and } A \subseteq B \}$ .

The Intuitionistic fuzzy  $\gamma$  supra interior of a set  $A$  is denoted by  $IF\gamma S-int(A)$  and is defined as

$IF\gamma S-int(A) = \cup \{ B : B \text{ is Intuitionistic fuzzy } \gamma \text{ supra open and } A \supseteq B \}$

**Definition 2.13[21]**

Let  $(X, \tau_\mu)$  and  $(Y, \sigma_\mu)$  be two Intuitionistic fuzzy supra topological spaces and let  $f: X \rightarrow Y$  be a function. Then  $f$  is said to be

- (i) Intuitionistic fuzzy supra continuous if the pre image of each Intuitionistic fuzzy supra open set of  $Y$  is an Intuitionistic fuzzy supra open set in  $X$ .
- (ii) Intuitionistic fuzzy supra closed if the image of each Intuitionistic fuzzy supra closed set in  $X$  is an Intuitionistic fuzzy supra closed set in  $Y$ .
- (iii) Intuitionistic fuzzy supra open if the image of each Intuitionistic fuzzy supra open set in  $X$  is an Intuitionistic fuzzy supra open set in  $Y$ .

**3. INTUITIONISTIC FUZZY  $\gamma$  SUPRA OPEN MAPPINGS**

**Definition 3.1**

A mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra open if the image of every Intuitionistic fuzzy  $\gamma$  supra open set of  $X$  is Intuitionistic fuzzy  $\gamma$  supra open set in  $Y$ .

**Remark 3.2**

Every Intuitionistic fuzzy  $\gamma$  supra open map is Intuitionistic fuzzy  $\gamma$  supra open but converse may not be true. For,

**Example 3.3** Let  $X = \{a, b\}$ ,  $Y = \{x, y\}$  and the Intuitionistic fuzzy set  $U$  and  $V$  are defined as follows

$$A_1 = \{x, \langle 0.7, 0.4 \rangle, \langle 0.5, 0.6 \rangle\},$$

$$A_2 = \{x, \langle 0.5, 0.6 \rangle, \langle 0.8, 0.7 \rangle\}$$

$$B_1 = \{y, \langle 0.7, 0.6 \rangle, \langle 0.5, 0.6 \rangle\},$$

$$B_2 = \{y, \langle 0.5, 0.6 \rangle, \langle 0.8, 0.7 \rangle\},$$

Then  $\tau_\mu = \{0\sim, 1\sim, A_1, A_2, A_1 \cup A_2\}$  and  $\sigma_\mu = \{0\sim, 1\sim, B_1, B_2, B_1 \cup B_2\}$  be Intuitionistic fuzzy supra topologies on  $X$  and  $Y$  respectively. Then the mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  defined by  $f(a) = x$  and  $f(b) = y$  is Intuitionistic fuzzy  $\gamma$  supra open but it is not Intuitionistic fuzzy supra open.

**Theorem 3.4**

A mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra open if and only if for every Intuitionistic fuzzy set  $U$  of  $X$   $f(S\text{-int}(U)) \subseteq IF\gamma S\text{-int}(f(U))$ .

**Proof:**

**Necessity** Let  $f$  be an Intuitionistic fuzzy  $\gamma$  supra open mapping and  $U$  is an Intuitionistic fuzzy supra open set in  $X$ . Now  $S\text{-int}(U) \subseteq U$  which implies that  $f(S\text{-int}(U)) \subseteq f(U)$ . Since  $f$  is an Intuitionistic fuzzy  $\gamma$  supra open mapping,  $f(S\text{-int}(U))$  is Intuitionistic fuzzy  $\gamma$  supra open set in  $Y$  such that  $f(S\text{-int}(U)) \subseteq IF\gamma S\text{-int}(f(U))$ .

**Sufficiency:** For the converse suppose that  $U$  is an Intuitionistic fuzzy supra open set of  $X$ . Then  $f(U) = f(S\text{-int}(U)) \subseteq IF\gamma S\text{-int}(f(U))$ . But  $IF\gamma S\text{-int}(f(U)) \subseteq f(U)$ . Consequently  $f(U) = IF\gamma S\text{-int}(f(U))$  which implies that  $f(U)$  is an Intuitionistic fuzzy  $\gamma$  supra open set of  $Y$  and hence  $f$  is an Intuitionistic fuzzy  $\gamma$  supra open.

**Theorem 3.5**

If  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is an Intuitionistic fuzzy  $\gamma$  supra open map then  $S\text{-int}(f^{-1}(G)) \subseteq f^{-1}(IF\gamma S\text{-int}(G))$  for every Intuitionistic fuzzy set  $G$  of  $Y$ .

**Proof:**

Let  $G$  is an Intuitionistic fuzzy set of  $Y$ . Then  $S\text{-int}(f^{-1}(G))$  is an Intuitionistic fuzzy supra open set in  $X$ . Since  $f$  is Intuitionistic fuzzy  $\gamma$  supra open  $f(S\text{-int}(f^{-1}(G)))$  is Intuitionistic fuzzy  $\gamma$  supra open in  $Y$  and hence  $f(S\text{-int}(f^{-1}(G))) \subseteq IF\gamma S\text{-int}(f(f^{-1}(G))) \subseteq IF\gamma S\text{-int}(G)$ . Thus  $S\text{-int}(f^{-1}(G)) \subseteq f^{-1}(IF\gamma S\text{-int}(G))$ .

**Theorem 3.6**

A mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra open if and only if for each Intuitionistic fuzzy set  $S$  of  $Y$  and for each Intuitionistic fuzzy supra closed set  $U$  of  $X$  containing  $f^{-1}(S)$  there is a Intuitionistic fuzzy  $\gamma$  supra closed  $V$  of  $Y$  such that  $S \subseteq V$  and  $f^{-1}(V) \subseteq U$ .

**Proof:**

**Necessity:** Suppose that  $f$  is an Intuitionistic fuzzy supra  $\gamma$  open map. Let  $S$  be the Intuitionistic fuzzy supra closed set of  $Y$  and  $U$  is an Intuitionistic fuzzy supra closed set of  $X$  such that  $f^{-1}(S) \subseteq U$ . Then  $V = (f^{-1}(U^c))^c$  is Intuitionistic fuzzy  $\gamma$  supra closed set of  $Y$  such that  $f^{-1}(V) \subseteq U$ .

**Sufficiency:** For the converse suppose that  $F$  is an Intuitionistic fuzzy supra open set of  $X$ . Then  $f^{-1}((f(F))^c) \subseteq F^c$  and  $F^c$  is Intuitionistic fuzzy supra closed set in  $X$ . By hypothesis there is an Intuitionistic fuzzy  $\gamma$  supra closed set  $V$  of  $Y$  such that  $(f(F))^c \subseteq V$  and  $f^{-1}(V) \subseteq F^c$ . Therefore  $F \subseteq (f^{-1}(V))^c$ . Hence  $V^c \subseteq f(F) \subseteq f((f^{-1}(V))^c) \subseteq V^c$  which implies  $f(F) = V^c$ . Since  $V^c$  is Intuitionistic fuzzy  $\gamma$  supra open set of  $Y$ . Hence  $f(F)$  is Intuitionistic fuzzy  $\gamma$  supra open in  $Y$  and thus  $f$  is Intuitionistic fuzzy  $\gamma$  supra open map.

**Theorem 3.7**

A mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra open if and only if  $f^{-1}(\gamma S\text{-cl}(B)) \subseteq S\text{-cl}(f^{-1}(B))$  for every Intuitionistic fuzzy set  $B$  of  $Y$ .

**Proof:**

**Necessity:** Suppose that  $f$  is an Intuitionistic fuzzy supra  $\gamma$  open map. For any Intuitionistic fuzzy set  $B$  of  $Y$   $f^{-1}(B) \subseteq S\text{-cl}(A)$   $f^{-1}(B)$  Therefore by theorem 6.3 there exists an Intuitionistic fuzzy  $\gamma$  supra closed set  $F$  in  $Y$  such that  $B \subseteq F$  and  $f^{-1}(F) \subseteq S\text{-cl}(A)$   $f^{-1}(B)$ . Therefore we obtain that  $f^{-1}(\gamma S\text{-cl}(B)) \subseteq f^{-1}(F) \subseteq S\text{-cl}(f^{-1}(B))$ .

**Sufficiency:** For the converse suppose that  $B$  is an Intuitionistic fuzzy set of  $Y$ . and  $F$  is an Intuitionistic fuzzy supra closed set of  $X$  containing  $f^{-1}(B)$ . Put  $V = S\text{-cl}(B)$ , then we have  $B \subseteq V$  and  $V$  is Intuitionistic fuzzy  $\gamma$  supra closed and  $f^{-1}(V) \subseteq S\text{-cl}(f^{-1}(B)) \subseteq F$ . Then by theorem 3.6  $f$  is Intuitionistic Intuitionistic fuzzy supra  $\gamma$  open.

**Theorem 3.8**

If  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  and  $g : (Y, \sigma_\mu) \rightarrow (Z, \rho_\mu)$  be two Intuitionistic fuzzy map and  $g \circ f : (X, \tau_\mu) \rightarrow (Z, \rho_\mu)$  is Intuitionistic fuzzy supra  $\gamma$  open. If  $g : (Y, \sigma_\mu) \rightarrow (Z, \rho_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra irresolute then  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra open map.

**Proof:**

Let  $H$  be an Intuitionistic fuzzy supra open set of Intuitionistic fuzzy supra topological space  $(X, \tau_\mu)$ . Then  $(g \circ f)(H)$  is Intuitionistic fuzzy  $\gamma$  supra open set of  $Z$  because  $g \circ f$  is Intuitionistic fuzzy supra  $\gamma$  open map. Now since  $g : (Y, \sigma_\mu) \rightarrow (Z, \rho_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra irresolute and  $(g \circ f)(H)$  is Intuitionistic fuzzy  $\gamma$  supra open set of  $Z$  therefore  $g^{-1}(g \circ f(H)) = f(H)$  is Intuitionistic fuzzy  $\gamma$  supra open set in Intuitionistic fuzzy supra topological space  $Y$ . Hence  $f$  is Intuitionistic fuzzy  $\gamma$  supra open map.

**4. INTUITIONISTIC FUZZY  $\gamma$  SUPRA CLOSED MAPPINGS**

**Definition 4.1**

A mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra closed if image of every Intuitionistic fuzzy  $\gamma$  supra closed set of  $X$  is Intuitionistic fuzzy  $\gamma$  supra closed set in  $Y$ .

**Remark 4.2**

Every Intuitionistic fuzzy  $\gamma$  supra closed map is Intuitionistic fuzzy  $\gamma$  supra closed but converse may not be true. For,

**Example 4.3**

Let  $X = \{a, b\}$ ,  $Y = \{x, y\}$  Then the mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  defined in Example 3.3 is Intuitionistic fuzzy  $\gamma$  supra closed but it is not Intuitionistic fuzzy supra closed.

**Theorem 4.4**

A mapping  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra closed if and only if for each Intuitionistic fuzzy set  $S$  of  $Y$  and for each Intuitionistic fuzzy supra open set  $U$  of  $X$  containing  $f^{-1}(S)$  there is a Intuitionistic fuzzy  $\gamma$  supra open set  $V$  of  $Y$  such that  $S \subseteq V$  and  $f^{-1}(V) \subseteq U$ .

**Proof:**

**Necessity:** Suppose that  $f$  is an Intuitionistic fuzzy  $\gamma$  supra closed map. Let  $S$  be the Intuitionistic fuzzy supra closed set of  $Y$  and  $U$  is an Intuitionistic fuzzy supra open set of  $X$  such that  $f^{-1}(S) \subseteq U$ . Then  $V = Y - f^{-1}(U^c)$  is Intuitionistic fuzzy supra  $\gamma$  open set of  $Y$  such that  $f^{-1}(V) \subseteq U$ .

**Sufficiency:** For the converse suppose that  $F$  is an Intuitionistic fuzzy supra closed set of  $X$ . Then  $(f(F))^c$  is an Intuitionistic fuzzy set of  $Y$  and  $F^c$  is Intuitionistic fuzzy supra open set in  $X$  such that  $f^{-1}((f(F))^c) \subseteq F^c$ . By hypothesis there is an Intuitionistic fuzzy  $\gamma$  supra open set  $V$  of  $Y$  such that  $(f(F))^c \subseteq V$  and  $f^{-1}(V) \subseteq F^c$ . Therefore  $F \subseteq (f^{-1}(V))^c$ . Hence  $V^c \subseteq f(F) \subseteq f((f^{-1}(V))^c) \subseteq V^c$  which implies  $f(F) = V^c$ . Since  $V^c$  is Intuitionistic fuzzy  $\gamma$  supra closed set of  $Y$ . Hence  $f(F)$  is Intuitionistic fuzzy  $\gamma$  supra closed in  $Y$  and thus  $f$  is Intuitionistic fuzzy  $\gamma$  supra closed map.

**Theorem 4.5**

If  $f : (X, \tau_\mu) \rightarrow (Y, \sigma_\mu)$  is Intuitionistic fuzzy supra closed and  $g : (Y, \sigma_\mu) \rightarrow (Z, \rho_\mu)$  is Intuitionistic fuzzy supra closed set. Then  $g \circ f : (X, \tau_\mu) \rightarrow (Z, \rho_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra closed set.

**Proof:**

Let  $H$  be an Intuitionistic fuzzy supra closed set of Intuitionistic fuzzy supra topological space  $(X, \tau_\mu)$ . Then  $f(H)$  is Intuitionistic fuzzy supra closed set of  $(Y, \sigma_\mu)$  because  $f$  is Intuitionistic fuzzy  $S$ -closed map. Now  $(g \circ f)(H) = g(f(H))$  is Intuitionistic fuzzy  $\gamma$  supra closed set in Intuitionistic fuzzy supra topological space  $Z$  because  $g$  is Intuitionistic fuzzy  $\gamma$  supra closed map. Thus  $g \circ f : (X, \tau_\mu) \rightarrow (Z, \rho_\mu)$  is Intuitionistic fuzzy  $\gamma$  supra closed set.

**REFERENCES**

- [1].M. E. Abd El-Monsef and A. E. Ramadan, On fuzzy supra topological spaces, Indian J. Pure and Appl. Math. no.4, 18(1987),322-329.
- [2].D. Andrijevic,  $b$  open sets, Math. Vesnik, 48(1) (1996), 59-64.
- [3]. Atnassova K., "Intuitionistic Fuzzy Sets", Fuzzy Sets and Systems, 20, 87-96,(1986).
- [4].Chang C.L. "Fuzzy Topological Spaces", J. Math. Anal. Appl. 24 182-190,(1968).
- [5] Coker, D. An introduction to Intuitionistic fuzzy topological spaces, Fuzzy Sets And Systems 88, 81-89, 1997.
- [6]. P.Deepika, S.Chandrasekar "Fine GS Closed Set and Fine SG Closed Sets in Fine topological Space", International Journal of Mathematics Trends and Technology (IJMTT).,V56(1):8-14 April 2018
- [7].P.Deepika, S.Chandrasekar , F-gs Open , F-gs Closed and F-gs Continuous Mappings in Fine Topological Spaces, International Journal of Engineering, Science and Mathematics, Vol.7 (4),April 2018, 351-359
- [8].P.Deepika, S.Chandrasekar , M. Sathyabama, Properties Of Fine Generalized Semi Closed Sets In Fine Topological Spaces, Journal Of Computer And Mathematical Sciences Vol 9 No.4 April (2018) 293-301
- [9].A.S. Mashhour, A.A.Allam, F.S. Mahmoud and F.H.Khedr, "On supra topological spaces" Indian J. Pure and Appl. vol. 4,14(1983),502-510.
- [10]. M. Parimala, C.Indirani, " Intuitionistic fuzzy  $\beta$ -supra open sets and Intuitionistic fuzzy  $\beta$ -supra continuous mapping", Notes on Intuitionistic fuzzy sets, 20(2014), 6-12.
- [11].M. Parimala, Jafari Saeid, Intuitionistic fuzzy  $\alpha$ -supra continuous maps,"Annals of fuzzy mathematics and informatics", vol.9, 5(2015), 745-751.
- [12].M. Parimala , C. Indirani, On Intuitionistic Fuzzy Semi - Supra Open Set and Intuitionistic Fuzzy Semi - Supra Continuous Functions Procedia Computer Science, 47 ,(2015),319-325.
- [13]. A.S. Mashhour, A.A.Allam, F.S. Mahmoud and F.H.Khedr, "On supra topological spaces", Indian J. Pure and Appl. vol.4,14(1983), 502-510.
- [14].Selvaraj Ganesan,SakkariVeeran Chandrasekar Another quasi  $\mu S$ -open and quasi  $\mu S$ -closed Functions,Journal of New Theory15,(2017),75-80.
- [15]. K.SafinaBegum,S.Chandarasekar ,Totally Fine Sg Continuous Functions And Slightly Fine Sg Continuous Functions In Fine Topological Spaces , International Journals Engineering ,Science & Mathematics (IJESM) , Vol 7 No4 April (2018),119-126.
- [16].K.SafinaBegum,,S.Chandarasekar, quasi fine sg open and quasi fine sg-closed functions in fine topological spaces ,Journal Of Computer And

- Mathematical Sciences ,Vol 9 No.,April (2018),  
245-253.
- [17] .S. Jeyashri,S.Chandrasekar,and M.Sathyabama,  
Soft b#-open Sets and Soft b#- continuous  
Functions in Soft Topological Spaces ,  
International Journal of Mathematics and  
its Applications,6(1-D)(2018), 651-658.
- [18].R.Selvaraj,S.Chandrasekar, Contra Supra\*g  
continuous Functions And Contra Supra\*g-  
Irresolute Functions In Supra Topological  
Spaces.ernational Journal of Engineering  
Science and Mathematics Vol. 7 I( 4),April  
2018, 127-133.
- [19] .K.SafinaBegum,S.Chandarasekar,Contra Fine  
Sg-Continuous Maps In Fine Topological Space,  
Journal of Global Research inMathematical  
Archives ,Vol.5,issue 4, 37-43,Apr-2018.
- [20].R.Selvaraj, S.Chandrasekar ,Supra\*g-Closed Sets  
in Supra Topological Spaces,International Journal  
of Mathematic Trends and Technology (IJMTT)  
,V56(1),15-20Apr- 2018.
- [21].N.Turnal,“On Intuitionistic Fuzzy Supra  
Topological spaces”, International Conference on  
Modeling and Simulation, Spain, vol.2, (1999)  
69-77.
- [22]. N. Turnal, “An over view of intuitionstic fuzzy  
Supra topological spaces”.Hacettepe Journal of  
Mathematics and Statistics, vol.32 (2003), 17-26.
- [23].Zadeh, L. A. “Fuzzy sets”, Information and  
Control, 8(1965), 338-353.